

# Muon Beams for Future Experiments

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Capabilities Frontier Workshop  
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# Disclaimer

- This is an overview and way too simplistic
- I will discuss this as an experimenter
- So therefore everything will not be even close to exactly right and all the definitions and boundaries are blurry.

# Physics Goals

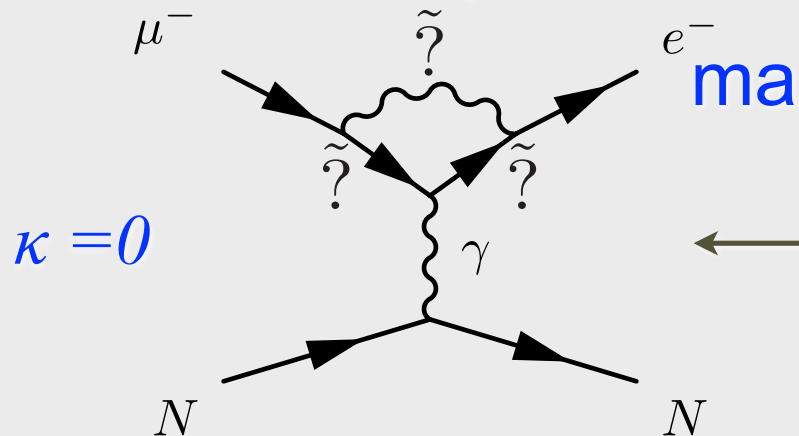
- What Experiments Do We Want To Do?
  - primarily charged lepton flavor violation (CLFV), muons changing into electrons without neutrino emission
$$\mu^+ \rightarrow e^+ \gamma \text{ and } \mu^+ \rightarrow e^+ e^+ e^-$$
$$\mu^+ e^- \rightarrow \mu^- e^+ \quad \mu^- N \rightarrow e^- N \text{ and } \mu^- N \rightarrow e^+ N(Z-2)$$
  - there are other things to measure but this is the killer app (IMO)
- What Is Our Goal?

“If you can measure something an order of magnitude better, you should do it” – Jim Cronin, who did some good experiments at BNL

# “Model-Independent” Form

$$\mathcal{L}_{\text{CLFV}} = \frac{m_\mu}{(\kappa + 1)\Lambda^2} \bar{\mu}_R \sigma_{\mu\nu} e_L F^{\mu\nu} + \frac{\kappa}{(1 + \kappa)\Lambda^2} \bar{\mu}_L \gamma_\mu e_L (\bar{u}_L \gamma_\mu u_L + \bar{d}_L \gamma_\mu d_L)$$

“Loops”

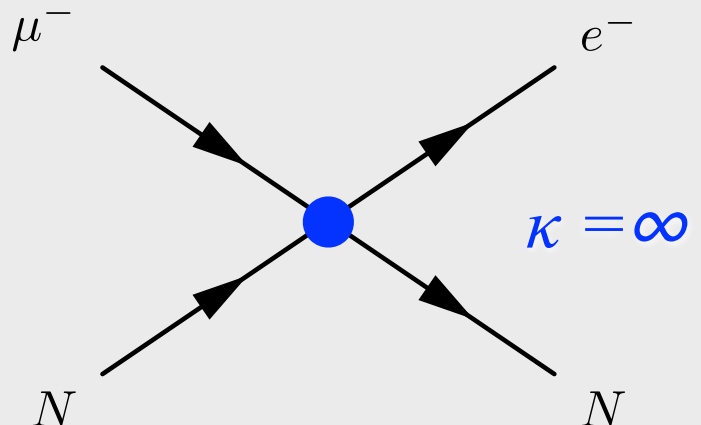


Supersymmetry and Heavy Neutrinos

Contributes to  $\mu \rightarrow e \gamma$   
(just imagine the photon is real)

“Contact Terms”

mass scale  $\Lambda$   
 $\kappa$



New Particles at High Mass Scale  
(leptoquarks, heavy Z,...)

Does not produce  $\mu \rightarrow e \gamma$

Quantitative Comparison?



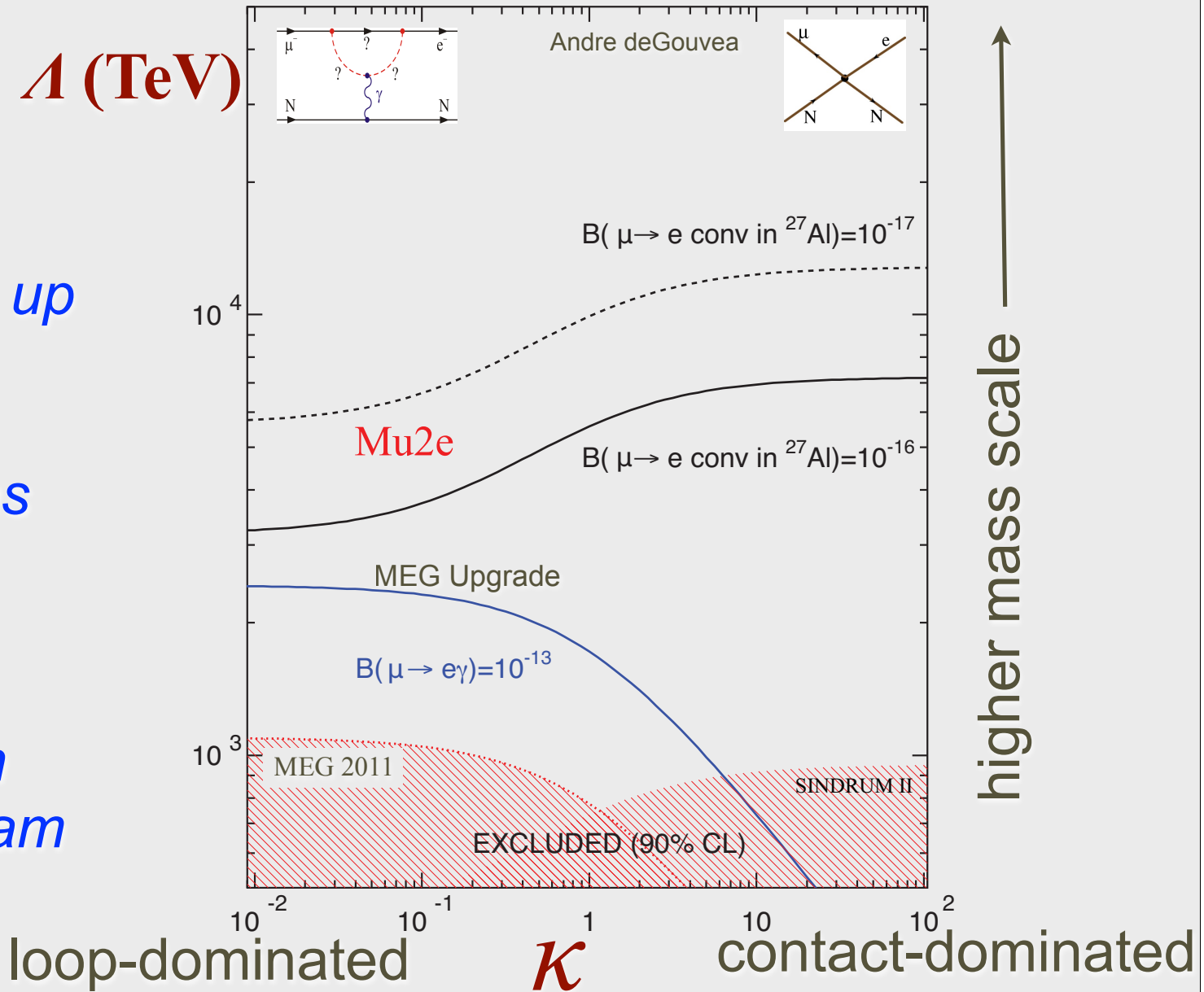
# $\mu e$ Conversion and $\mu \rightarrow e \gamma$

CLFV:

*probes masses up  
to  $10^4 \text{ TeV}/c^2$*

*next generations  
are discovery  
experiments*

*new beams can  
build rich program*

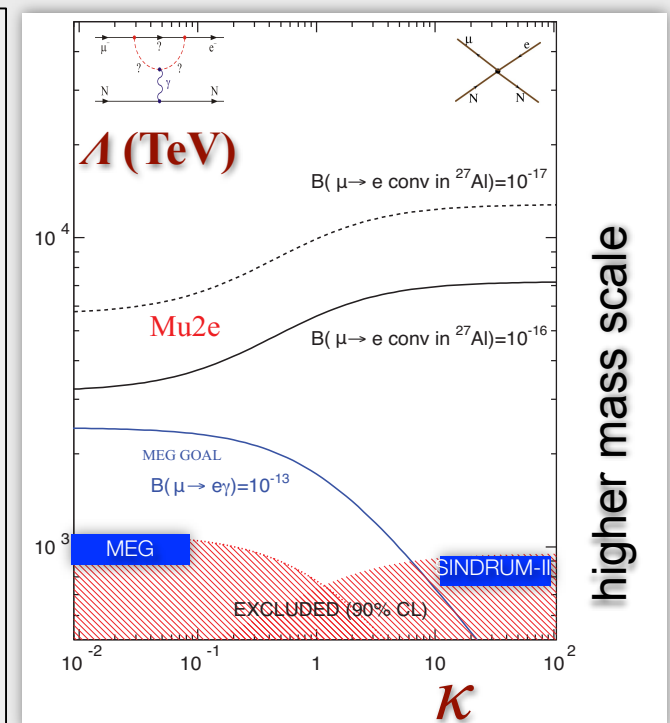
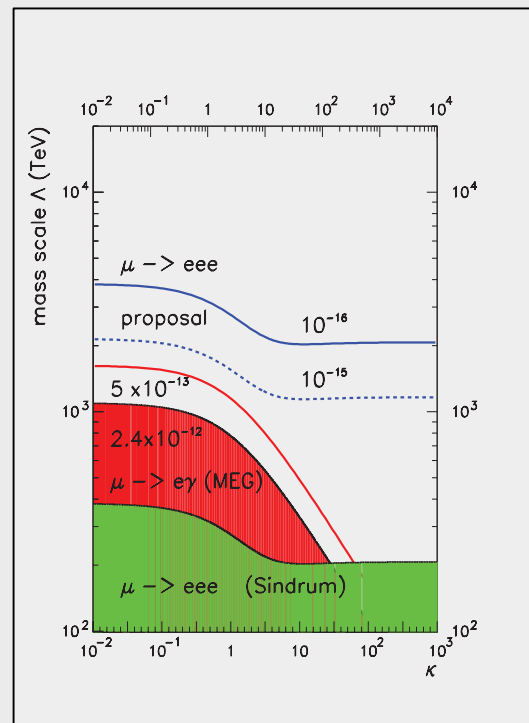
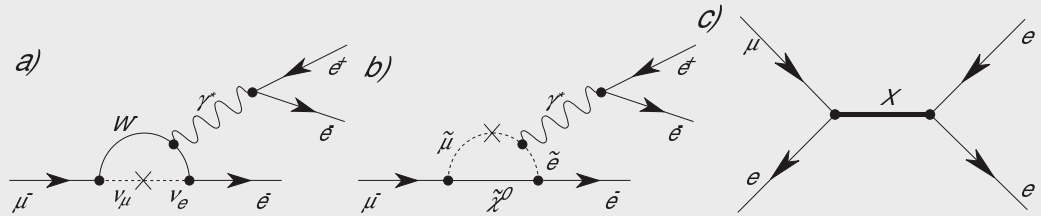


$$\mu \rightarrow 3e$$

$$L_{\text{eff}} = \frac{m_\mu}{\Lambda^2} \bar{e} (\sigma^{\mu\nu} F^{\mu\nu}) \mu + \frac{1}{\Lambda_F^2} \bar{e} \Gamma_A e \bar{e} \Gamma_A \mu + \frac{1}{\Lambda_F'^2} \bar{q} \Gamma_A q \bar{e} \Gamma_A \mu$$

Hisano

- “Sister” process to  $\tau \rightarrow 3l$
- The meaning of  $\kappa$  is not the same since the underlying diagrams are different, but still indicative
- *reaching “ultimate” sensitivity, limited by radiative background, may require surface muon beams to get sufficient statistics*



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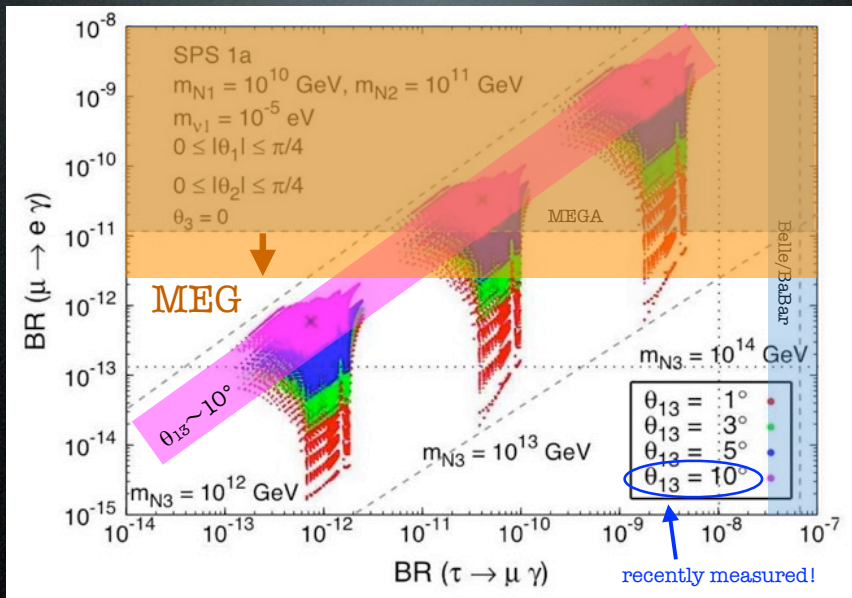
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# Specific Examples

## Implication of Large $\theta_{13}$

→ larger  $\text{BR}(\mu \rightarrow e \gamma)$



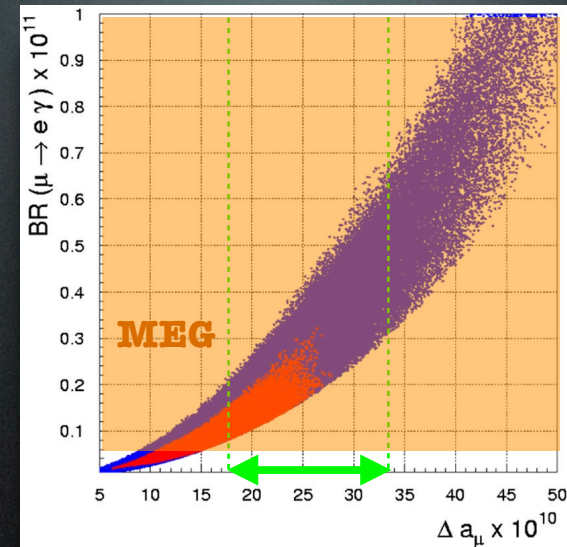
S. Antusch et al. JHEP11 (2006) 090

with BNL821 g-2

Combining MEG at PSI

with  $\tau \rightarrow \mu \gamma$

muon (g-2) anomaly



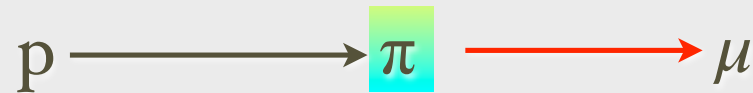
G. Isidori et al. PRD75, 115019

muon's anomalous magnetic moment

# Surface Muon Beams

“Arizona Beam”

A. Pifer et al., NIM 135, 39.



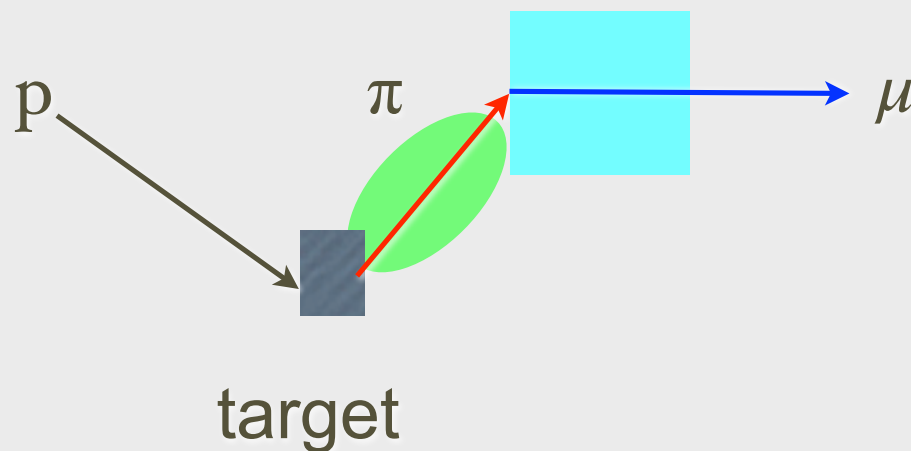
- Pions range out and decay close to the surface of a target and yield muons at 29.8 MeV/c (MEG may go slightly sub-surface; see below eqn.)
  - Source is very well defined
  - Polarization (pion stopped) near 100%
  - $\mu^+$  only since  $\pi^-$  would be captured on nuclei
  - positron contamination

$$R_{\mu} \sim p^{3.5} \sqrt{\left(3.5 \frac{\Delta p}{p}\right)^2 + \left(\Delta R_{\text{straggling}}\right)^2}$$

# Cloud Muon Beams

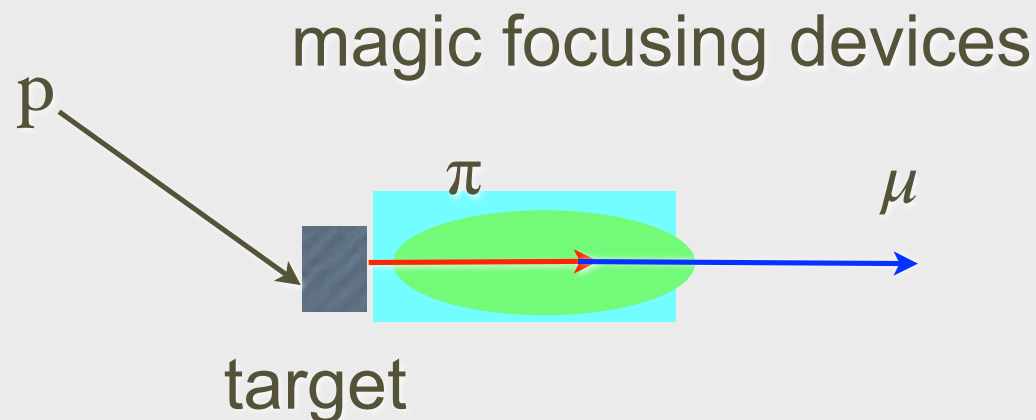
“surface beam” but pion decays outside target

magic focusing devices



- Large momentum range
- Source bigger than production target
- Contamination of both charges of pions and electrons
- Low Polarization

# Decay Muon Beams



- Source much bigger than production target
  - Polarization high; by using pion lifetime, contamination low
  - Very flexible
    - neutrino horn beams
    - many DIS experiments
- “cloud beam” but select pion momentum*



# Experiments

- Reorder the experiments into beam type:

- two stopped muon processes: *stopped* → +

$$\mu^+ \rightarrow e^+ \gamma \text{ and } \mu^+ \rightarrow e^+ e^+ e^-$$

- two captured muon processes in clouds

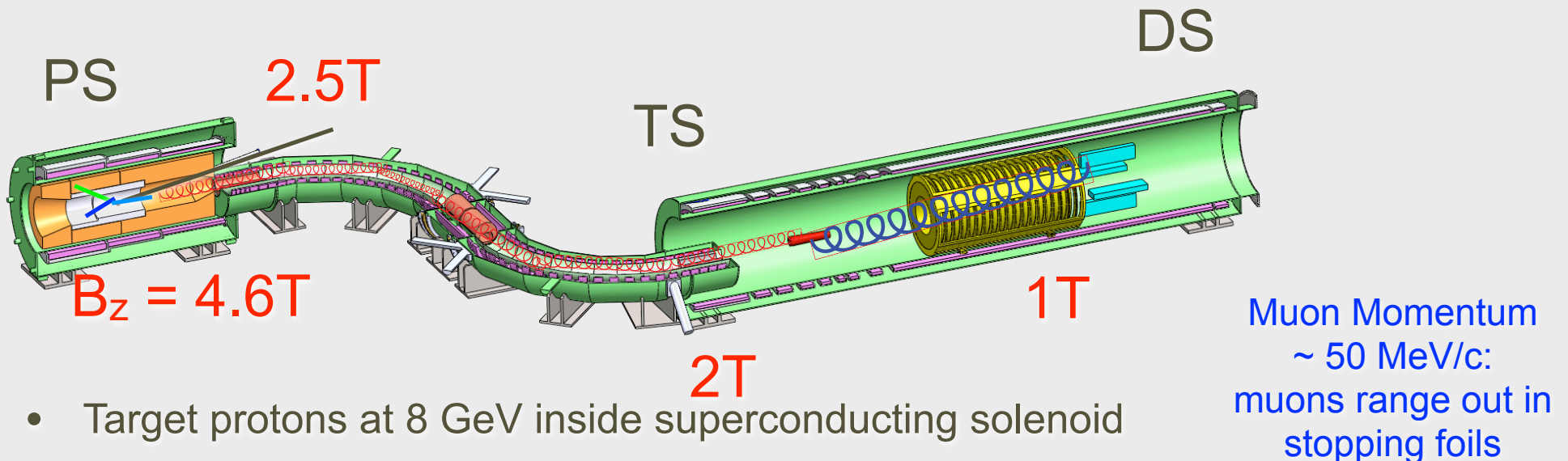
$$\mu^- N \rightarrow e^- N \text{ and } \mu^- N \rightarrow e^+ N(Z-2) \quad \textit{captured} \rightarrow -$$

- muonium-antimuonium oscillation and muonium HFS from cloud beam

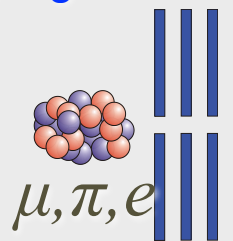
$$\mu^+ e^- \rightarrow \mu^- e^+$$

# Mu2e Muon Beam: Three Solenoids and Gradient

4.6T  $\longrightarrow$  B-field gradient  $\longrightarrow$  1T



- Target protons at 8 GeV inside superconducting solenoid
- Capture muons and guide through S-shaped region to Al stopping target
- Gradient fields used to collect and transport muons



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# To Pulse or Not To Pulse?

- Pulses:
  - width of pulse
  - time between pulses
  - shape of pulse
  - “extinction”: suppress beam between pulses
- In general (but NOT a fine line)
  - stopped muon experiments want as DC a beam as possible to keep instantaneous rates low
  - capture muon experiments want varying pulse width and separation depending on lifetime in capture atom

# What Exists?

<http://arxiv.org/pdf/1301.7225v2.pdf>

Laboratory / Beam line	Energy / Power	Present Surface $\mu^+$ rate (Hz)	Future estimated $\mu^+/\mu^-$ rate (Hz)
PSI (CH)	(590 MeV, 1.3 MW, DC)		
LEMS	"	$4 \cdot 10^8$	
$\pi E 5$	"	$1.6 \cdot 10^8$	
HiMB	(590 MeV, 1 MW, DC)		$4 \cdot 10^{10}(\mu^+)$
J-PARC (JP)	(3 GeV, 1 MW, Pulsed) currently 210 KW		
MUSE D-line	"	$3 \cdot 10^7$	
MUSE U-line	"		$4 \cdot 10^8(\mu^+)$ (2012)
COMET	(8 GeV, 56 kW, Pulsed)		$10^{11}(\mu^-)$ (2019/20)
PRIME /PRISM	(8 GeV, 300 kW, Pulsed)		$10^{11-12}(\mu^-)$ (> 2020)
FNAL (USA)			
Mu2e	(8 GeV, 25 kW, Pulsed)		$5 \cdot 10^{10}(\mu^-)$ (2019/20)
Project X Mu2e	(3 GeV, 750 kW, Pulsed)		$2 \cdot 10^{12}(\mu^-)$ (> 2022)
TRIUMF (CA)	(500 MeV, 75 kW, DC)		
M20	"	$2 \cdot 10^6$	
KEK (JP)	(500 MeV, 2.5 kW, Pulsed)		
Dai Omega	"	$4 \cdot 10^5$	
RAL -ISIS (UK)	(800 MeV, 160 kW, Pulsed)		
RIKEN-RAL		$1.5 \cdot 10^6$	
RCNP Osaka Univ. (JP)	(400 MeV, 400 W, Pulsed)		
MUSIC	currently max 4W		$10^8(\mu^+)$ (2012) means > $10^{11}$ per MW
DUBNA (RU)	(660 MeV, 1.65 kW, Pulsed)		
Phasatron Ch.I-III		$3 \cdot 10^4$	

# Examine Some Experiments

closely related experimentally to  $\mu^+ \rightarrow e^+ e^+ e^-$

- MEG:  $\mu^+ \rightarrow e^+ \gamma$

PSI: ~51 MHz , 300 psec wide

- need to stop muons and let them decay
- signal is back-to-back photon and electron

$$\mathcal{B} \propto \overset{\text{why DC}}{\left(\frac{R_\mu}{D}\right)} (\Delta t_{e\gamma}) \frac{\Delta E_e}{m_\mu/2} \overset{\text{why well-defined stop}}{\left(\frac{\Delta E_\gamma}{15m_\mu/2}\right)^2} \left(\frac{\Delta\theta_{e\gamma}}{2}\right)^2$$

- R/D term is rate over duty cycle: want DC beam as constant as possible over macroscopic time
- $\Delta\theta_{e\gamma}$  is vertexing: surface muons, well-defined stop location

<http://arxiv.org/pdf/1301.7225v2.pdf>

# What Do They Have Now?

should  
regard this  
as a  
challenge

## A. The MEG beam line and muon target

A schematic of the MEG beam line and the  $\pi E5$  channel is shown in Fig. 11. Driven by the world's most intense DC proton machines at the Paul Scherrer Institut's high-intensity proton accelerator complex HIPA, it constitutes the intensity frontier in continuous muon beams around the world (c.f. Table II) and as such, is capable of delivering more than  $10^8 \mu^+ / s$  at 28 MeV/c to the MEG experiment. The surface muon beam has distinct advantages over a conventional 2-step pion decay-channel.

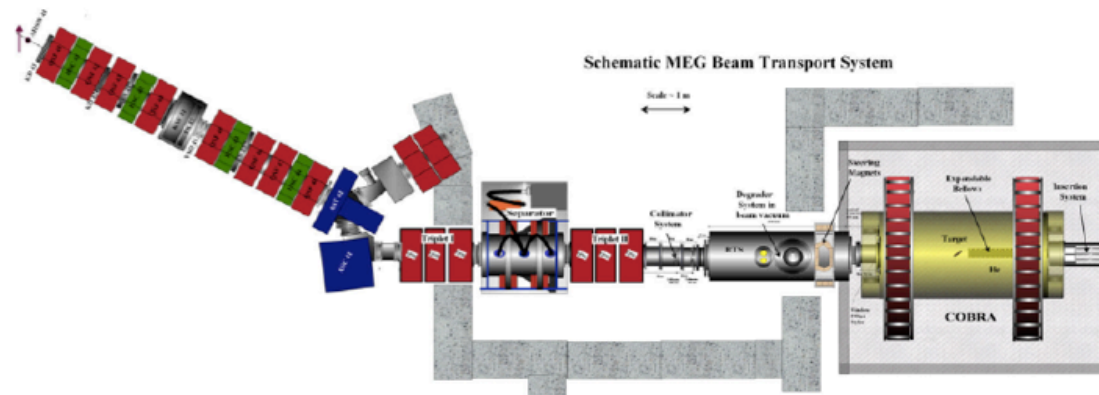


FIG. 11: (Left-part) shows the  $\pi E5$  channel, connecting the production target  $E$  to the  $\pi E5$  area. The MEG beam line starts from the extraction element Triplet I exiting the wall, followed by a Wien-filter, Triplet II and a collimator system, used to eliminate the beam contamination. The final range adjustment and focusing is performed by a superconducting solenoid BTS, before the muons are stopped in an ultra-thin target placed at the centre of the COBRA positron spectrometer.

# What Would We do Next?

- How Do We Progress?
  - just-approved MEG upgrade is x10 from existing: beyond that?
- This is pure speculation and my personal opinion:
  - convert the photon and use tracking
  - limits from tracking, not calorimetry
- But you lose a lot of rate, since converter must be thin or experiment will suffer from multiple scattering

# Rough Guesses

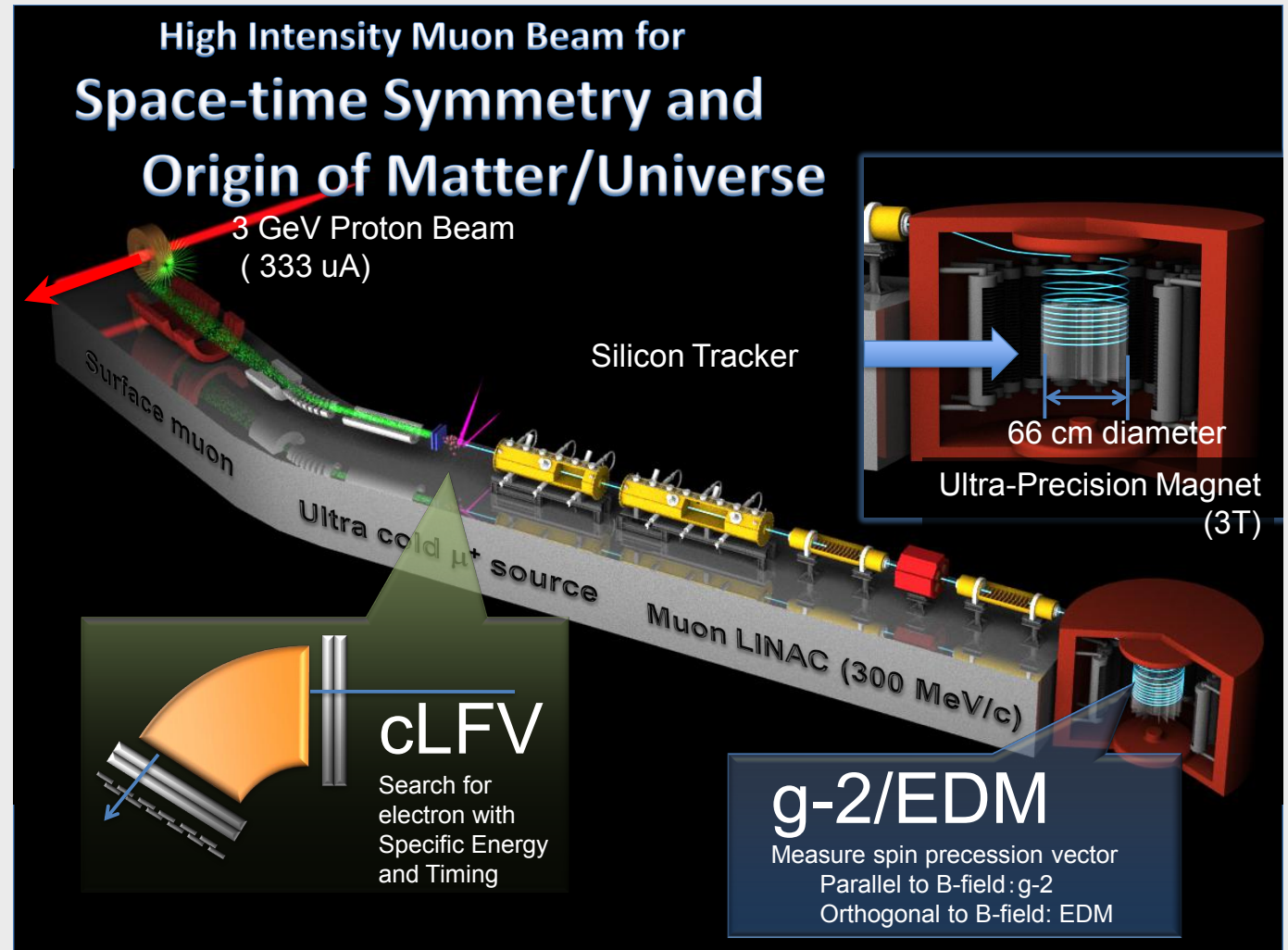
- $10^{11}$  stopped muons/sec
- surface or sub-surface positive muon beam
  - recall  $R \sim p^{3.5}$  so small drop in momentum is big change in range, helps with vertex
- as continuous as possible (10-20 nsec rep rate probably fine)
- proton energy? don't care for MEG but matters for Mu2e (pbars) -- so experiment-dependent

# Muon Spin Rotation

- See <https://indico.fnal.gov/conferenceDisplay.py?confId=6025>
- Applications in
  - materials science
  - condensed matter
  - chemistry
- don't have time or knowledge to discuss

# Japanese Plans

- different  $g-2$  technique
  - “cold  $g-2$ ”, not magic momentum
- CLFV:  
DeeMe, separate from COMET and x100 less sensitive
- and EDMs



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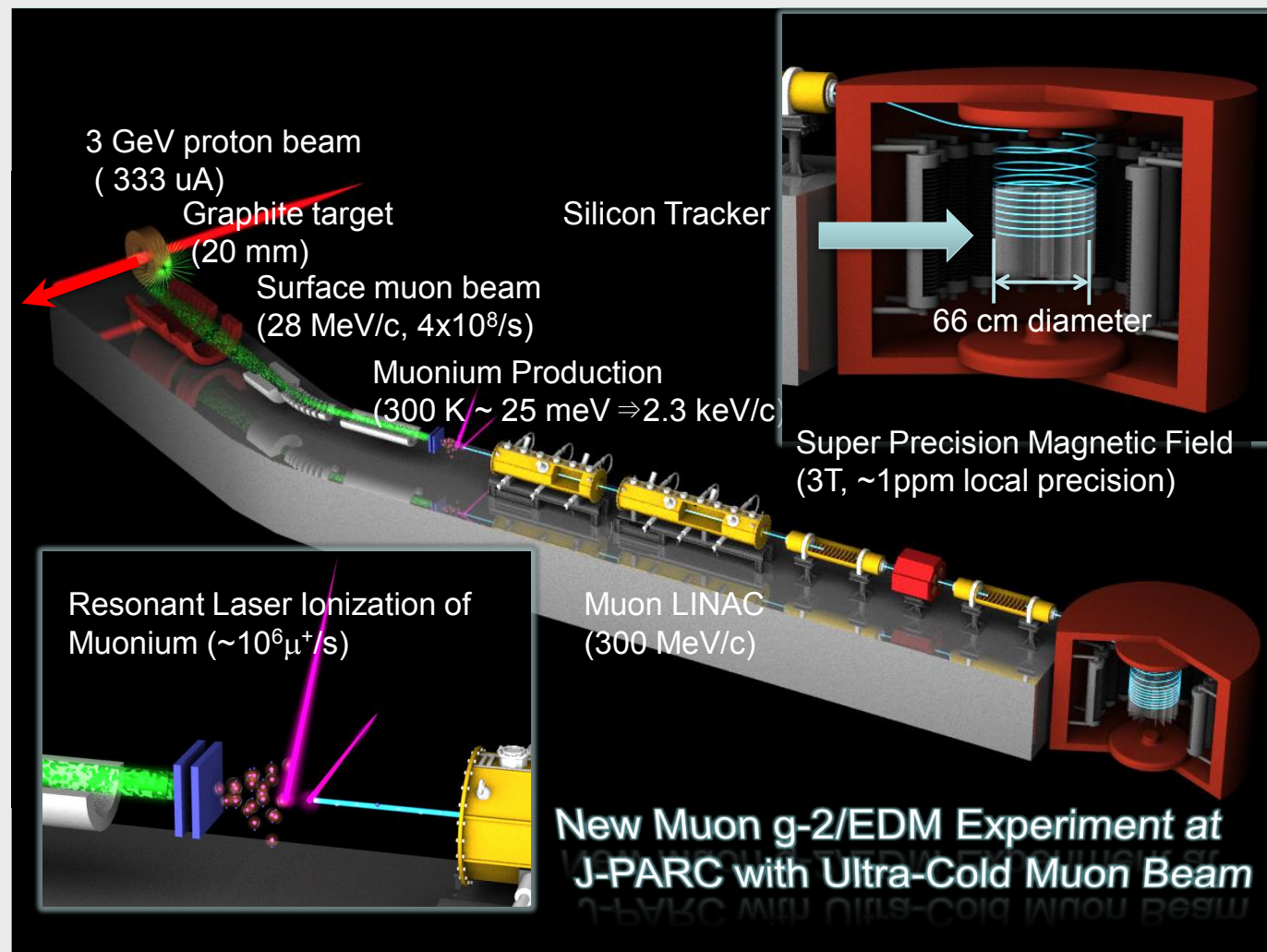
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# Status: Much to Work On!

- yield of muonium too low to be useful; precise numbers hard to get
- surface muon rate way too low for competitive next-gen expt in CLFV



U.S losing in pretty picture department

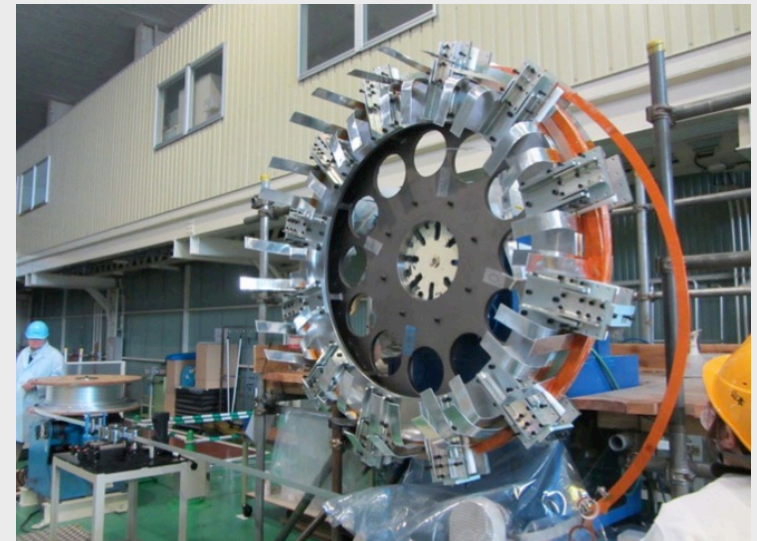
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# Mu2e: Status

- US Mu2e at CD1 planning for CD2 winter 2013
- Data ~2020
- Prototyping underway
  - 3 km of test cable in fall 2013



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# Next-Gen Mu2e

- Will Current Method Work?
  - depends on a lot

probably ~ x10  
with some  
improvements/  
experience



need big changes

# Limits: non-beam

- Cosmic Ray Backgrounds
  - make it deeper, just money
- Decay-in-Orbit Spectrum
  - intrinsic physics background, overcome with resolution and statistics

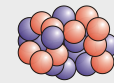
# Beam Related Limits

- Must understand one key background: radiative pion capture (RPC)
- No time to discuss details, but antiprotons also make RPC if they arrive at experiment
  - 8 GeV KE booster makes pbars
  - 3 GeV below threshold; probably best
  - 1 GeV probably fine

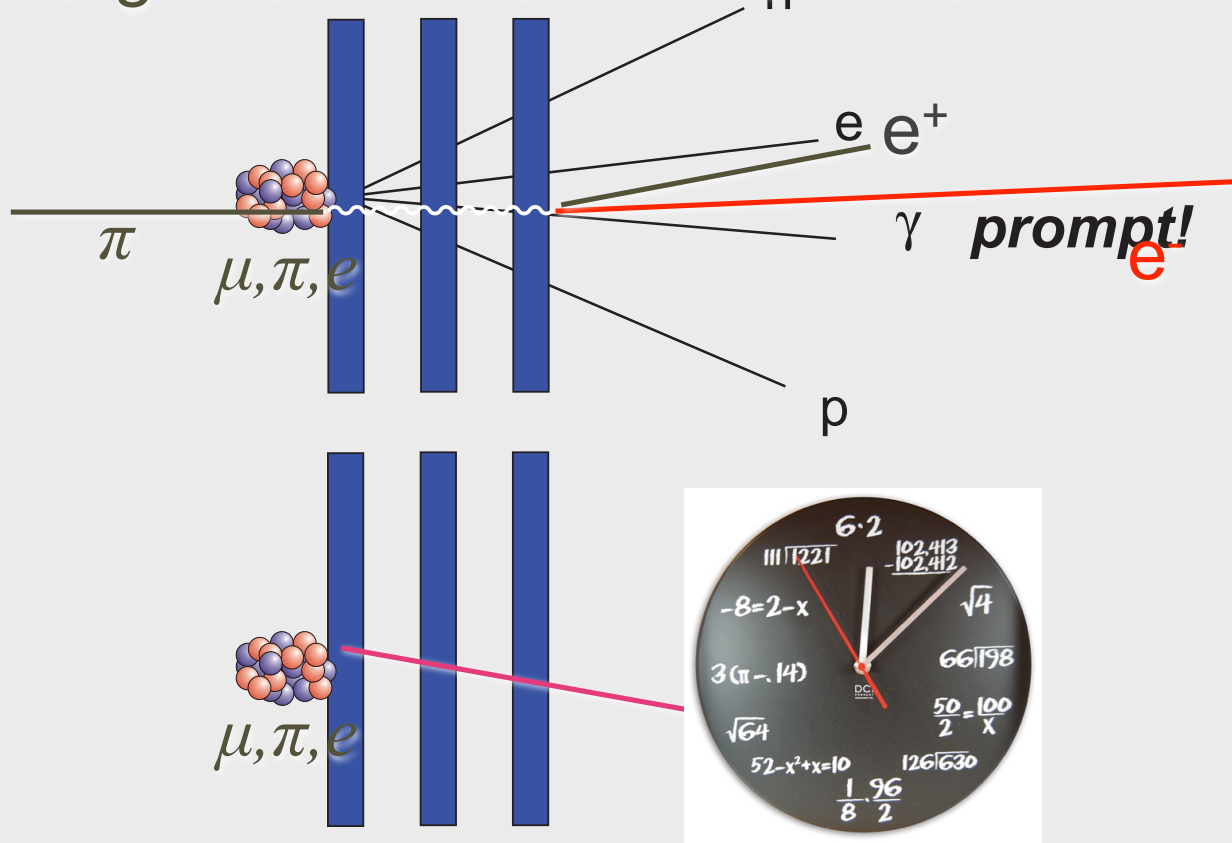


# Prompt backgrounds and Pulsed Beam

target foils: muon converts here



= muons, electrons, pions



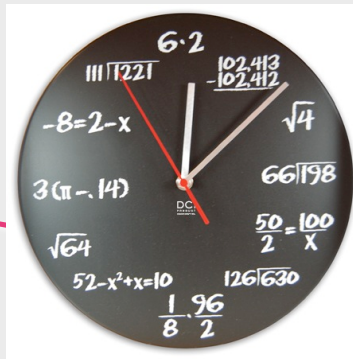
pulsed beam lets us wait until after prompt backgrounds disappear and rate lowered

Radiative Pion Capture:

$$\pi N \rightarrow \gamma N$$

$$\gamma \rightarrow e^+ e^- \text{ in foils}$$

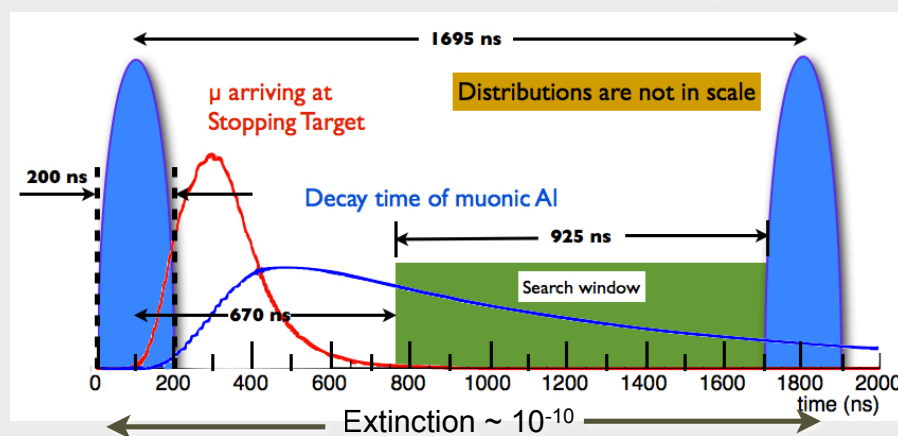
delayed 105 MeV electron



# Pulsed Beam Structure

- Tied to prompt rate and machine: FNAL “perfect”
- Want **pulse duration  $\ll \tau_{\mu}^{Al}$**  , **pulse separation  $\approx \tau_{\mu}^{Al}$** 
  - FNAL Debuncher has circumference  **$1.7\mu\text{sec}$**  ,  $\sim x2 \tau_{\mu}^{Al}$
- Extinction between pulses  $< 10^{-10}$  needed

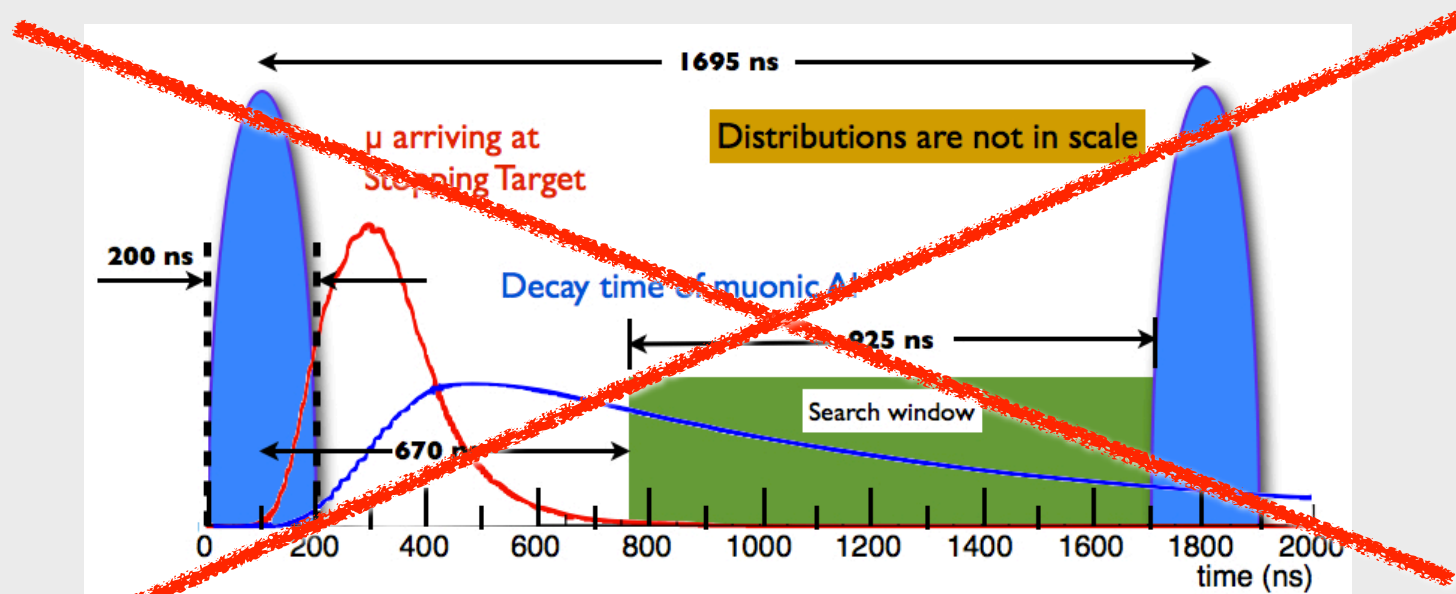
= # protons out of pulse / # protons in pulse



- $10^{-10}$  based on simulation of prompt backgrounds and beamline

# What Has to Change?

- If we see a signal, need to go to higher  $Z$
- Lifetime of the captured muon decreases with higher  $Z$
- For Au, lifetime = 72.6 nsec: *inside beam pulse!*





# Different Muon Beams

<http://www.sciencedirect.com/science/article/pii/S0920563211005330>

- Would like to let all pions decay and then extract muons: no background, no extinction...
- Would be even better if muons nearly monochromatic: tightly controlled stopping location
  - PRISM/PRIME idea at J-PARC
    - FFAG kicker not on mass shell yet
  - Other ideas?
    - Do they lead to neutrino factory/muon collider?

# PRISM=Phase Rotated Intense Slow Muon source

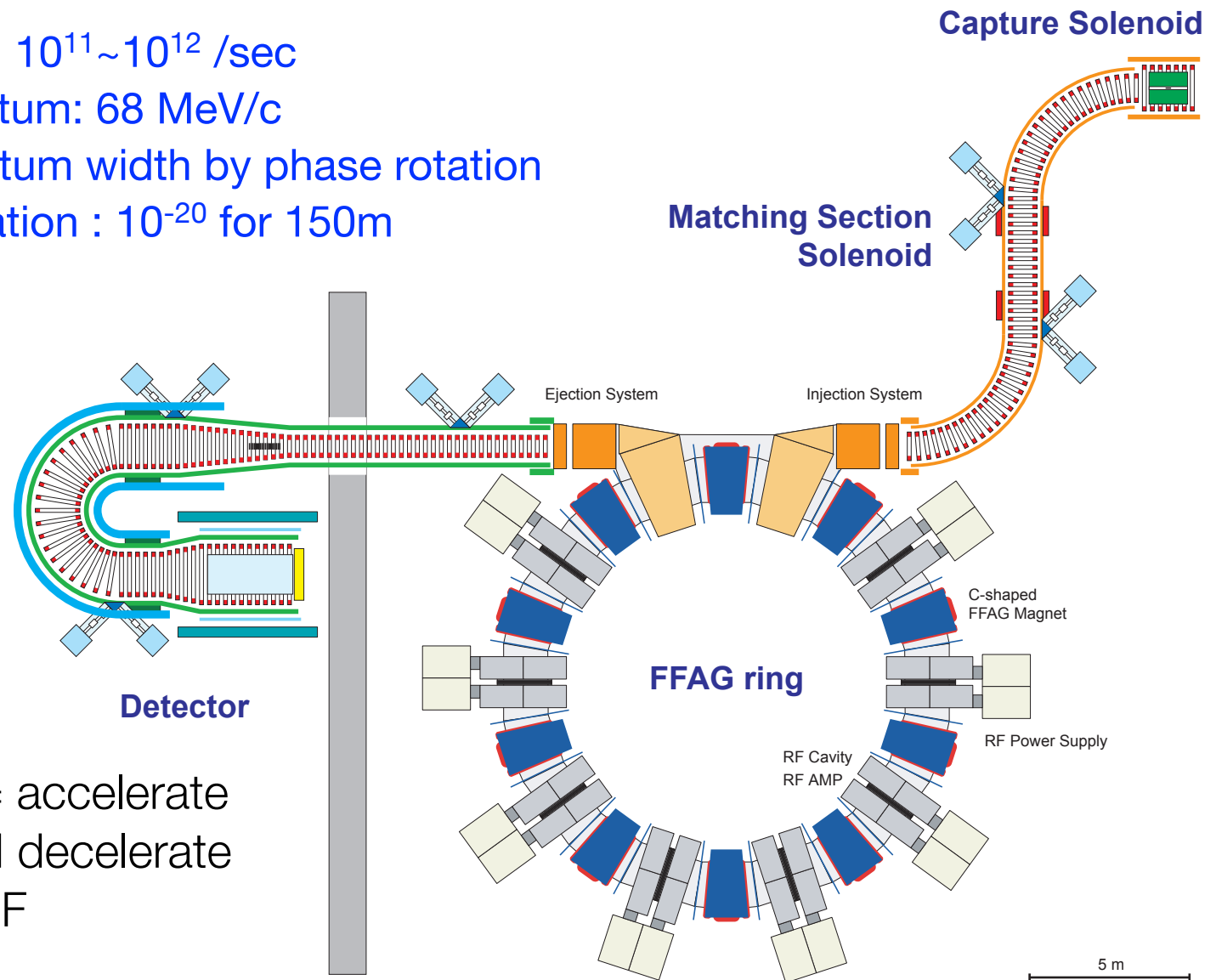
## PRISM

$$B(\mu^- + Ti \rightarrow e^- + Ti) < 10^{-18}$$

- muon intensity:  $10^{11} \sim 10^{12}$  /sec
- central momentum: 68 MeV/c
- narrow momentum width by phase rotation
- pion contamination :  $10^{-20}$  for 150m

Table 1  
Accelerator Parameters of the PRISM system.

<b>Proton Beam</b>	
Beam power	0.75 - 2 MW
Beam Kinetic Energy	2-8 GeV
Bunch length at the target	15 ns total
Repetition rate	1 KHz
<b>Target &amp; <math>\pi/\mu</math> transport</b>	
Target Type	Solid
Capture Elements	Solenoid 4-10 T
Transport System	solenoidal channel & FFAG transport line
Beam Polarity	Negative
<b>PRISM ring</b>	
Machine type	FFAG
Momentum Acceptance	$\pm 20$ %
Reference muon momentum	40-50 MeV/c
Acceptance (H/V)	$(3.8/0.57) \pi$ cm rad
Harmonic number	1
RF Voltage per turn	5.5 MV
RF frequency	3-6 MHz
Injection/extraction type	single turn
Extraction Kicker Rise Time	50-60 ns
Repetition Rate	1 KHz
Initial momentum spread	$\pm 20$ %
Final momentum spread	$\pm 2$ %
No. of turns	6
Synchrotron oscillations	$\frac{1}{4}$ or $\frac{3}{4}$



Phase rotation = accelerate slow muons and decelerate fast muons by RF

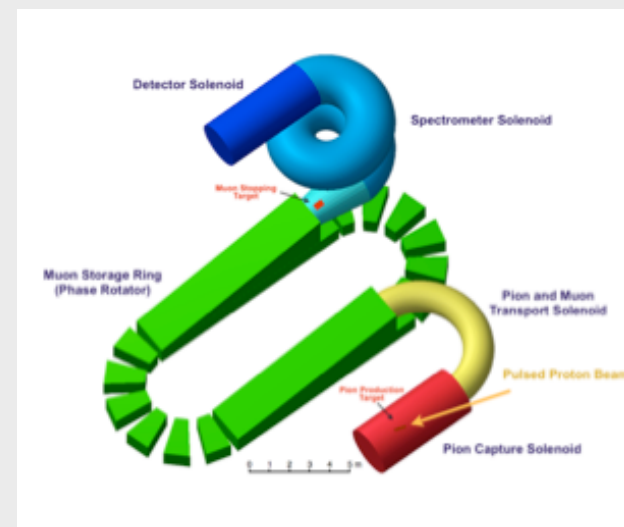
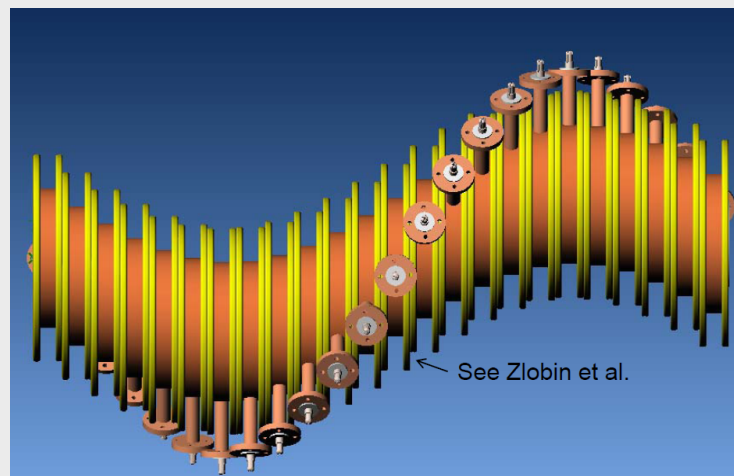
# Other Ideas

- Racetrack FFAG

J. B. Lagrange et al, Straight Section in Scaling FFAG Accelerator, Proc. PAC09, FRF5PFP002, Vancouver, Canada, 2009

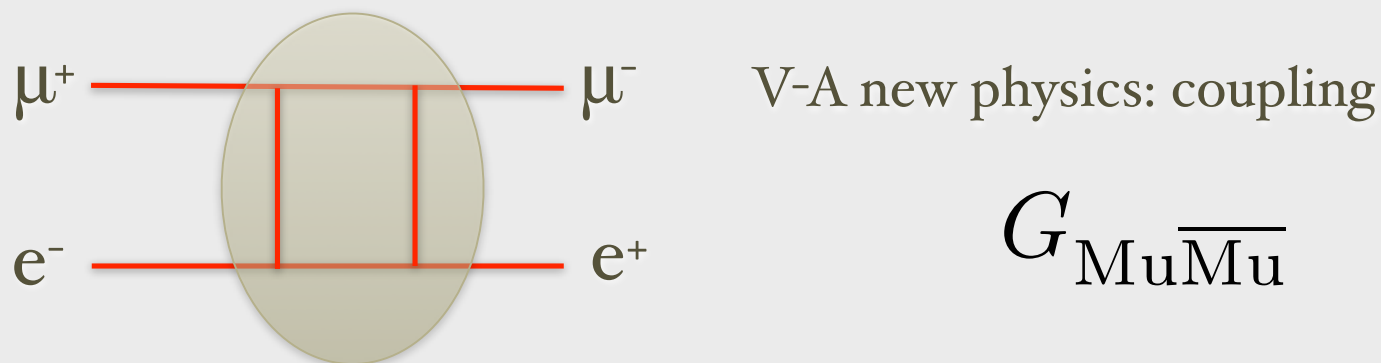
- HCC

- Other?



- <http://projectx-docdb.fnal.gov/cgi-bin/ShowDocument?docid=996>

# Muonium/AntiMuonium



$$G_{\text{Mu}\overline{\text{Mu}}}$$

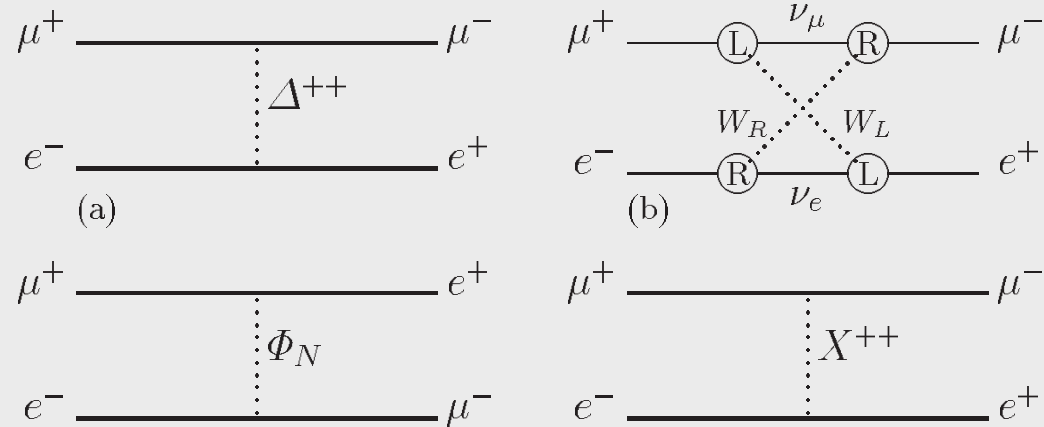
- World's best limit from PSI : (Willmann, L., Jungmann, K. et al.(1999), Phys. Rev. Lett. 82, 49)

$$\Delta L = 2$$

$$G_{\text{Mu}\overline{\text{Mu}}} < 3 \times 10^{-3} G_F \text{ (Probability of spon. transition } < 8.2 \times 10^{-11})$$

- Wide variety of Beyond Standard Model Physics
- Could be improved x100 with better resolution and pulsed beam, so  $\sim 10^{-5} G_F$

# Muonium-Antimuonium

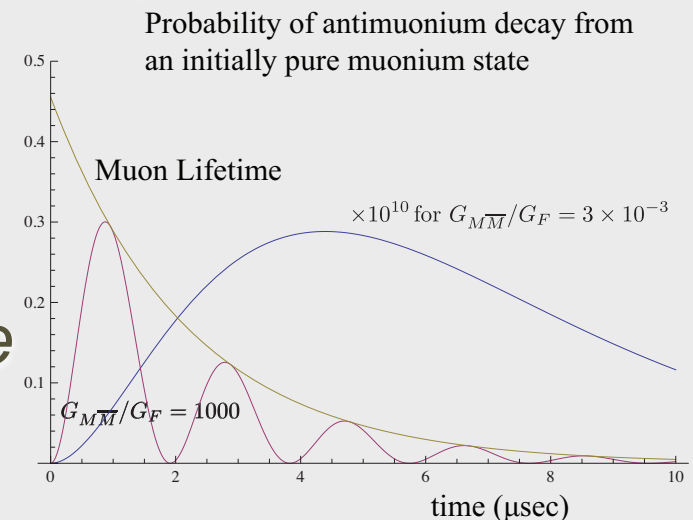


- Number of models

- doubly charged Higgs, heavy Majorana neutrinos, ...

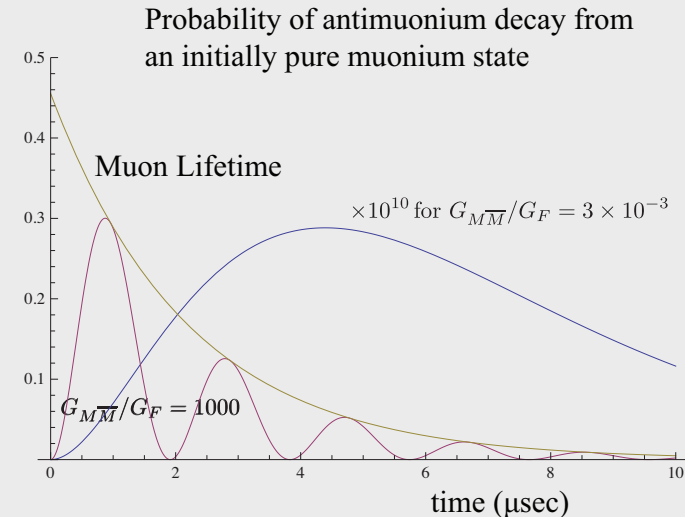
- oscillates like  $K^0 - \bar{K}^0$

- *but damped by muon lifetime*



# Time-Behavior

- Prepare muonium
- Look for positrons vs. time
  - positron left behind after negative muon decay at “1s” energy of 13.5 eV
- But there’s a muon decay background:
  - $\mu^+ \rightarrow e^+ e^- e^+ 2\nu$
  - sometimes the electron is background



# So Pulse Beam to Suppress Muon Decay

- Wait enough muon lifetimes to suppress decays
- Want pulses (somewhat arbitrary) five muon lifetimes apart
- then the rest is the detector resolution
- should be able to do x100 better(from discussions with people who did last generation)
- muonium yield requirement not as stringent as cold g-2, should be manageable

# Summary

- One accelerator? Multiple Accelerators?
  - that's for you to decide
- Sociological Comment: in neutrino world, get a big advantage from multiple neutrino experiments at one site; similar constructive interference between g-2 and Mu2e
  - grad student/post-doc pipeline
  - easier to build a program
  - well-demonstrated at PSI



# Conclusions: Beam Requirements

- Wide variety of beams required
  - pulse rates, muon energy, etc. vary
- Flexibility and Power are most important drivers

Physics Process	Continuous/Pulsed	Capture /Stopped	$\sim \#$ Muons	Muon KE
$\mu \rightarrow 3e$	continuous	stopped	$\mathcal{O}(10^{18})$	surface
$\mu \rightarrow e\gamma$	continuous	stopped	$\mathcal{O}(10^{18})$	surface
$\mu^- N \rightarrow e^- N$	pulsed	capture	$\mathcal{O}(10^{23})$	$\leq 50$ MeV
$\mu^- N \rightarrow e^+ N(A, Z - 2)$	pulsed	capture	$\mathcal{O}(10^{21})$	$\leq 50$ MeV
$\mu^+ e^- \rightarrow \mu^- e^+$	pulsed	stopped	$\mathcal{O}(10^{15})$	surface

*these are very rough numbers*